SAFE SUPERSYMMETRY BREAKING

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Introduction

Renormalisable SO(10) GUTs need large representations

Neutrino mass: $16126_H 16$

(alternatively $16 \ 16_H \ 16_H \ 16$ - nonrenormalisable)

In supersymmetry this means the appearance of Landau pole below Planck scale

Example: $3 \times 16 + 126_H + \overline{126}_H + 210_H + 10_H$

Clark, Kuo, Nakagawa, '82

Aulakh, Mohapatra, '83

Aulakh, BB, Melfo, Senjanović, Vissani, hep-ph/0306242

For some time it was the minimal renormalisable supersymmetric SO(10)

until it was found that neutrino masses are too small

Aulakh, hep-ph/0506291

BB, Melfo, Senjanović, Vissani, hep-ph/0511352

Aulakh, Garg, hep-ph/0512224

Bertolini, Schwetz, Malinsky, hep-ph/0605006

For us this is an irrelevant detail, we will consider this model as a prototype, toy model of

consistent asymptotically UV interacting (=SAFE) susy GUT

$$b_{1-loop} = -3 \times 8 + (3 \times 2 + 56 + 35 + 35 + 1) = 109$$

and so the Landau pole is obtained from the solution of

$$\frac{dg_{10}}{d\log\mu} = \frac{b_1}{(4\pi)^2} g_{10}^3$$

$$\to g_{10}^2(\mu) = \frac{g_{10}^2(\mu_0)}{1 - \frac{g_{10}^2(\mu_0)}{8\pi^2} b_1 \log\left(\frac{\mu}{\mu_0}\right)}$$

The solution diverges when

$$g_{10}^2(\mu_{\rm Landau\ pole}) = \infty$$
 \rightarrow

$$\mu_{\text{Landau pole}} = M_{GUT} \exp\left(\frac{8\pi^2}{b_1 g_{10}^2(M_{GUT})}\right) \approx 4 \times M_{GUT} \ll M_{Planck}$$

What happens there?

Higher loops could save the situation and make the theory UV safe

Litim, Sannino, 1406.2337

I.e. higher loops change the 1-loop infinite result, making all couplings finite, although nonzero (the theory is not UV free!)

This is the UV analogue of the Banks Zaks IR fixed point

Banks, Zaks, '82

But perturbation theory is not applicable here, 1-loop large, 2-loops even larger, etc

All one can do in a supersymmetric theory is to look for possible fixed points and check if various non-perturbative constraints (positivity bounds) are satisfied.

The main one is on the a-central charge:

$$a_{UV} \ge a_{IR}$$

There is a prescription how to calculate this central charge in susy:

$$a = \sum_{i} a_1(R_i)$$

with

$$a_1(R) = 3(R-1)^3 - (R-1)$$

and R_i the R-charge of the superfield i

If all known constraints are satisfied, the fixed point is allowed.

A candidate for such UV fixed point has been found, assuming first generation of matter superfields has zero yukawas.

All fields except 16_1 have R = 2/3

$$R_{16_1} = \frac{113}{6}$$

Then

$$a_{UV} - a_{IR} = 2.72 \times 10^5 > 0$$

and the fixed point is a consistent candidate for a UV safe theory

Bajc, Sannino, 1610.09681

The massless first generation is clearly a problem, but we will not dwell on it further here. We assume this can be somehow corrected.

What we are interested here is in the supersymmetry breaking.

In fact in the IR one needs the SM, which is not supersymmetric. So susy has to be broken somehow. The above picture did not consider it. The purpose here is to show how to break it without destroying the existence of the UV safe fixed point.

We will use here an implementation, employed for SU(5),

Bajc, Melfo, 0801.4349

of an earlier idea for dynamical supersymmetry breaking

Witten, '81

Dimopoulos, Dvali, Rattazzi, Giudice, hep-ph/9705307

The idea is the following: take two gauge non-singlets $\phi_{1,2}$:

$$W_{sb} = \mu \phi_1 \phi_2 + \lambda \phi_1^2 \phi_2 + \dots$$

Supersymmetric minimum:

$$\frac{\partial W_{sb}}{\partial \phi_1} = 0 \quad \to \quad \phi_2 = 0$$

$$\frac{\partial W_{sb}}{\partial \phi_2} = 0 \quad \to \quad \phi_1 = -\frac{\mu}{\lambda}$$

Non-supersymmetric extremum:

$$\frac{\partial W_{sb}}{\partial \phi_1} = 0 \quad \to \quad \phi_1 = -\frac{\mu}{2\lambda}$$

$$\frac{\partial W_{sb}}{\partial \phi_2} = -\frac{\mu^2}{4\lambda} \quad \to \quad \phi_2 \quad \text{undetermined}$$

At this point not clear yet if a minimum or a maximum (ϕ_2 classical flat direction)

But susy is broken so radiative corrections will lift the potential

$$V = \frac{|F_2|^2}{Z_2(\phi_2)}$$

 $F_2 = \frac{\partial W}{\partial \phi_2} \approx \text{const...} \text{ susy breaking } F\text{-term of } \phi_2$

 $Z_2(\phi_2)$... wave function renormalisation of ϕ_2

Imagine we add in our SO(10) model two 54 (2-index symmetric):

$$W_{sb} = \mu Tr \left(\phi_1 \phi_2\right) + \lambda Tr \left(\phi_1^2 \phi_2\right) + \dots$$

$$\phi_{1,2} = 54_{1,2}$$

What is $Z_2(\phi_2)$?

It can be computed as an RGE:

$$\frac{d(\log Z_2)}{d\tau} = 20g_{10}^2 - \frac{28}{5}\lambda^2$$

$$\tau = \frac{\log\left(\phi_2\right)}{8\pi^2}$$

We need now to add two more RGEs:

$$\frac{dg_{10}^2}{d\tau} = 133g_{10}^4$$

$$\frac{d(\log \lambda^2)}{d\tau} = -60g_{10}^2 + 28\lambda^2$$

Closed system of RGEs for $g_{10}(\phi_2)$, $\lambda(\phi_2)$, $Z_2(\phi_2)$

The extremum of the potential

$$\frac{\partial V}{\partial \phi_2} = -\frac{|F_2|^2}{Z_2^2} \frac{\partial Z_2}{\partial \phi_2}$$

vanishes when

$$\frac{\partial Z_2}{\partial \phi_2} = 0 \to \lambda^2 = \frac{20}{\frac{28}{5}} g_{10}^2$$

The second derivative of the potential at the extremum

$$\frac{\partial^2 V}{\partial \phi_2^2} = -\frac{|F_2|^2}{Z_2^2} \frac{\partial^2 Z_2}{\partial \phi_2^2}$$

is positive if $\frac{\partial^2 Z_2}{\partial \phi_2^2} < 0$

However this is not the case for our situation:

$$\frac{\partial^2 Z_2}{\partial \phi_2^2} > 0$$

and the potential has a maximum.

Can we use something else instead of 54? The two fields $\phi_{1,2}$ needs to have both quadratic and cubic gauge invariants. Another possibility is for example 210. It turns out that it is even worse, i.e. bigger the representation more positive the second derivative of Z_2 in the extremum

Our SO(10) model cannot be used to break supersymmetry this way.

However we know that in SU(5) two $24_{1,2}$ can break supersymmetry, i.e. their superpotential

$$W = \mu Tr \left(\phi_1 \phi_2\right) + \lambda Tr \left(\phi_1^2 \phi_2\right) + \dots$$

$$\phi_{1,2} = 24_{1,2}$$

develops a susy breaking minimum of the potential

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What we need is thus to spontaneously break $SO(10) \rightarrow SU(5)$ first

The superpotential with 210_H , 126_H , $\overline{126}_H$, 10_H has a minimum in the SU(5) direction

BB, Melfo, Senjanović, Vissani, hep-ph/0402122

Fukuyama, Ilakovac, Kikuchi, Meljanac, Okada, hep-ph/0405300 One problem is left:

$$54 = 24 + 15 + \overline{15}$$

and the two extra $15 + \overline{15}$ pairs makes the SU(5) theory blow up before reaching the SO(10) scale. To avoid it, we add a 45 representation and the term

$$\Delta W = Tr \, (45 \, 54_1 54_2)$$

Being 45 two index antisymmetric, the 45 vev gives mass to the two $15 + \overline{15}$ pairs leaving just the two $24_{1,2}$ light

Coupling this new 45 with the other Higgs representations $(210_H, 126_H, \overline{126}_H, 10_H)$ does not spoil the SU(5) minimum.

Fukuyama, Ilakovac, Kikuchi, Meljanac, Okada, hep-ph/0405300

Last comment:

only two 54 are not enough. In fact the dots ... in

$$W_{sb} = \mu Tr \left(54_1 54_2 \right) + \lambda Tr \left(54_1^2 54_2 \right) + \dots$$

mean actually higher dimensional operators (otherwise some states remain light, in contrast with the requirement for unification).

... terms are obtained by integrating out two other heavy $54_{3,4}$

The complete susy breaking superpotential has four $54_{1,2,3,4}$:

$$W_{csb} = Tr (M54_354_4 + 54_3 (\mu_1 54_1 + \lambda_1 54_1^2) + 54_4 (\mu_2 54_2 + \lambda_2 54_1 54_2))$$

Bajc, Melfo, 0801.4349

At this point we have to check if the new model, i.e. with

- 4 extra 54 dimensional SO(10) representations
- 1 extra 45 dimensional SO(10) representations

on top of the original

$$3 \times 16 + 210_H + 126_H + \overline{126}_H + 10_H$$

still has an allowed UV fixed point

It is easy to determine the R-charges of the new fields from the new superpotential terms plus a-maximisation yielding

$$R(54_{1,2,3,4}) = R(45) = \frac{2}{3}$$

This does not change by itself the value of the a-central charge but through new contributions to the NSVZ relation

$$\sum_{i} T_i(R_i - 1) = 0$$

the new fields change the value of

$$R(16_1) = \frac{169}{9}$$

with then

$$a_{UV} - a_{IR} = 961950 > 0$$

still compatible with all positivity constraints.

Thus this SO(10) model is able to break supersymmetry and have a UV fixed point.

Conclusions

- supersymmetric renormalisable SO(10) have a Landau pole much before the Planck scale
- consistent candidates (susy SO(10)) for a UV fixed point are known from the literature
- supersymmetry breaking cannot be obtained directly in SO(10) but the model must first be broken into SU(5)
- although details slightly change, the UV fixed point of such model is still consistent